



Bs Mixing and Lifetime Difference at CDF

Pierluigi Catastini
(INFN Pisa and Siena University)

On behalf of the CDF Collaboration

SUSY09 - Boston, MA
June 6, 2009.

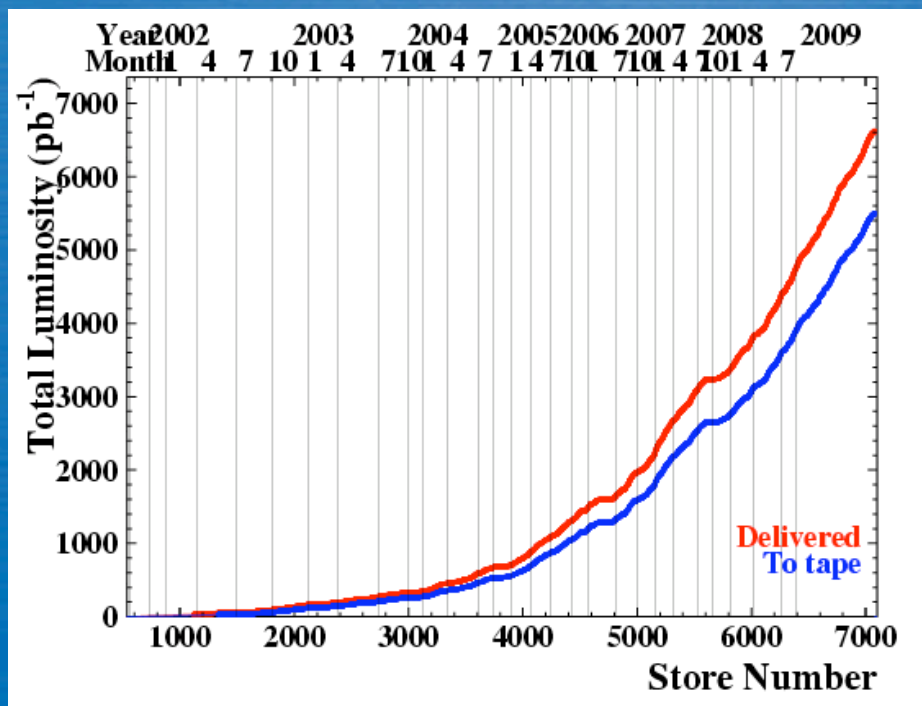
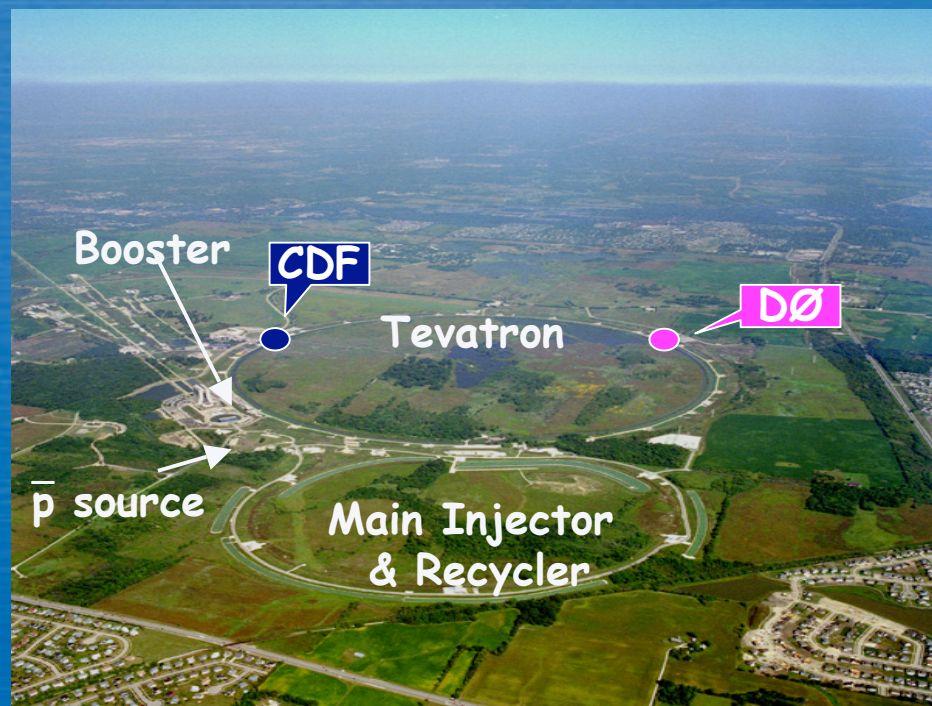


Outline

- Tevatron and CDF II
 - $B_s \rightarrow D_s D_s$
 - $B_s \rightarrow K K$
 - $B_s \rightarrow J/\psi \varphi \longrightarrow \beta_s$
- $\Delta\Gamma$ {
- B_s Mixing
 - For Flavor Tagging calibration to be used in $B_s \rightarrow J/\psi \varphi$

Tevatron at Fermilab

- $p\bar{p}$ collisions at 1.96 TeV
- All b hadron species produced:
 $B, B_s, B_c, \Lambda_b, \Sigma_b, \Xi_b, \Omega_b \dots$
- more than 5 fb^{-1} data on tape for each experiment
- Show analyses $\leq 2.8 \text{ fb}^{-1}$ of data



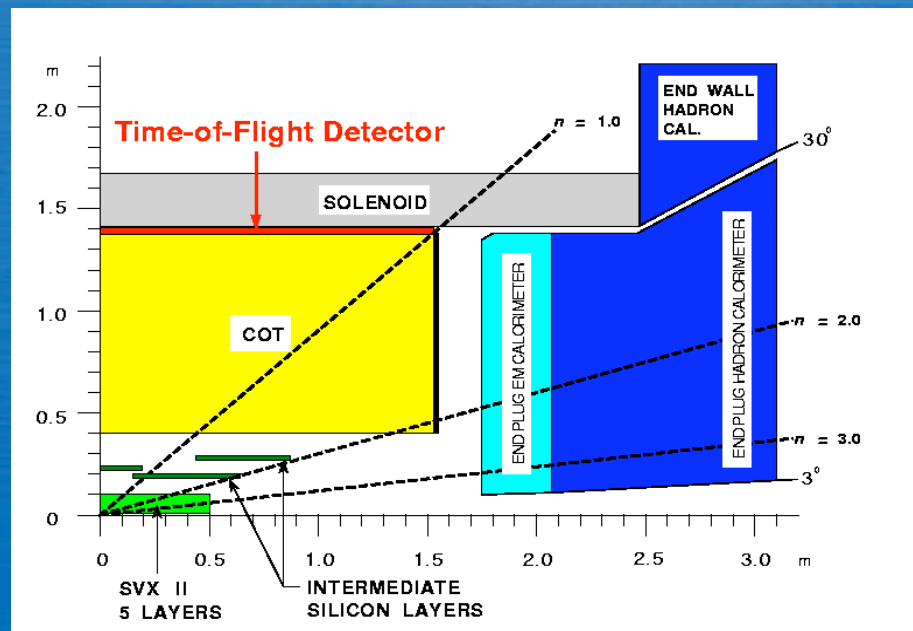
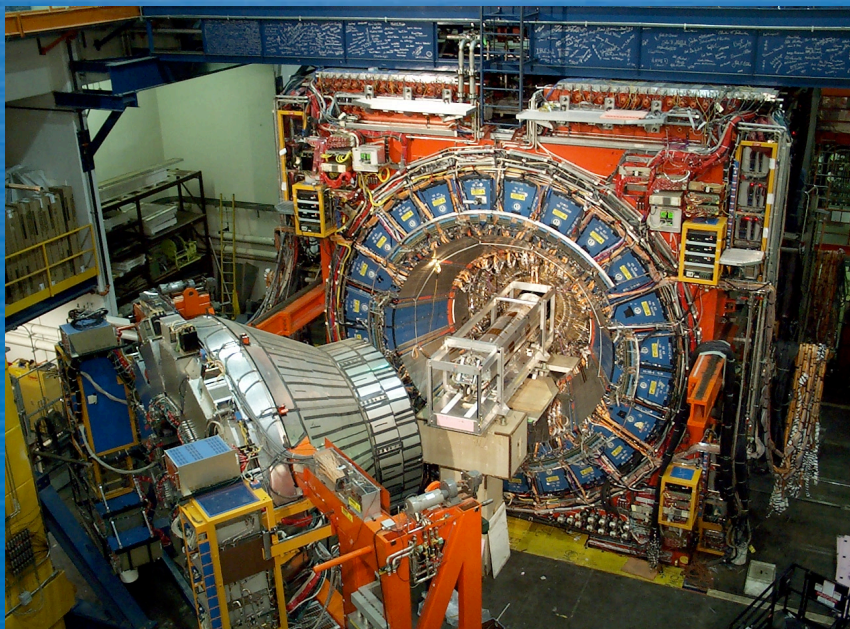
CDF II Detector

TRACKING system:

- Drift Chamber 96 layers ($|\eta| < 1$)
particle ID with dE/dx
- Silicon Tracker (L00+SVX+ISL, up to $|\eta| \approx 2$)
I.P. resolution $35 \mu\text{m}$ at 2 GeV

In Addition:

- Particle identification: dE/dx and TOF
- Electron and muon ID by calorimeters and muon chambers



Neutral B_s System

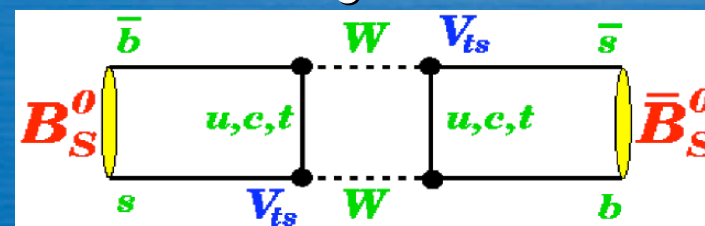
- Time evolution of B_s flavor eigenstates described by Schrodinger equation:

$$i \frac{d}{dt} \begin{pmatrix} B_s^0(t) \\ \bar{B}_s^0(t) \end{pmatrix} = H \begin{pmatrix} B_s^0(t) \\ \bar{B}_s^0(t) \end{pmatrix} \equiv \underbrace{\begin{pmatrix} M_0 & M_{12} \\ M_{12}^* & M_0 \end{pmatrix}}_{\text{mass matrix}} - \frac{i}{2} \underbrace{\begin{pmatrix} \Gamma_0 & \Gamma_{12} \\ \Gamma_{12}^* & \Gamma_0 \end{pmatrix}}_{\text{decay matrix}} \begin{pmatrix} B_s^0(t) \\ \bar{B}_s^0(t) \end{pmatrix}$$

- Diagonalize mass (M) and decay (Γ) matrices
→ mass eigenstates :

$$|B_s^H\rangle = p|B_s^0\rangle - q|\bar{B}_s^0\rangle \quad |B_s^L\rangle = p|B_s^0\rangle + q|\bar{B}_s^0\rangle$$

- Flavor eigenstates differ from mass eigenstates and mass eigenvalues are different ($\Delta m_s = m_H - m_L \approx 2|M_{12}|$)



- Mass eigenstates have different decay widths
 $\Delta \Gamma = \Gamma_L - \Gamma_H \approx 2|\Gamma_{12}| \cos(\phi_s)$ where

$$\phi_s = \arg \left(-\frac{M_{12}}{\Gamma_{12}} \right) \approx 4 \times 10^{-3}$$

$\Delta\Gamma$: Lifetime Difference

$$\Delta\Gamma = \Gamma_L - \Gamma_H$$



CP Specific: $B_s \rightarrow D_s D_s$

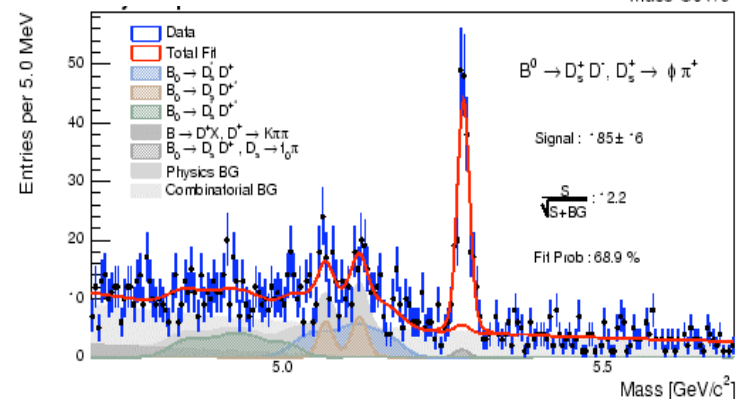
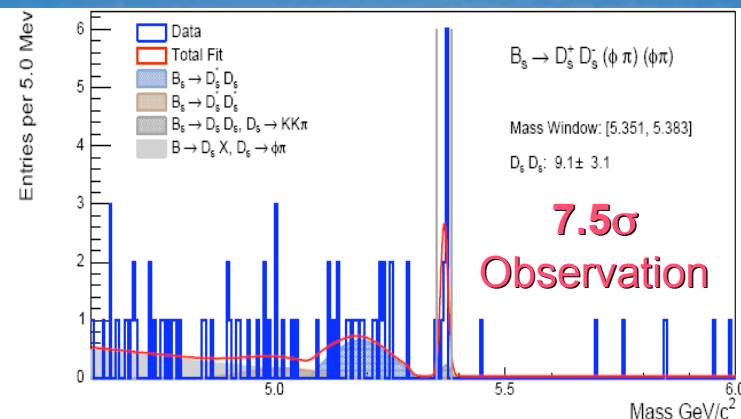
- Assume no CP violation: $B_s^L = \text{CP even}$, $B_s^H = \text{CP odd}$
- $b \rightarrow ccs$ decay (e.g. $B_s \rightarrow D_s D_s$) is pure CP even
- Thus a lifetime measurement of $B_s \rightarrow D_s D_s$ would measure Γ_L

HOWEVER

- Branching ratio is related to $\Delta\Gamma/\Gamma$ and if neglect small CP odd component:

$$\frac{\Delta\Gamma}{\Gamma} = 2Br(B_s^0 \rightarrow D_s^{(*)-} D_s^{(*)+})$$

- $BR(B_s \rightarrow D_s D_s)$ measured relative to $B^0 \rightarrow D_s D^-$
- Three D_s decay modes reconstructed in each case



**In
355 pb⁻¹**

$$\frac{BR(B_s^0 \rightarrow D_s D_s)}{BR(B_d^0 \rightarrow D_s D^-)} = 1.44_{-0.31}^{+0.38} (stat)_{-0.12}^{+0.08} (sys) \pm 0.21 \left(\frac{f_s}{f_d} \right) \pm 0.20 (BR)$$

CP Specific: $B_s \rightarrow D_s D_s$

With $355 \text{ pb}^{-1} \rightarrow 95\% \text{ C.L.}$:

$$\frac{\Delta\Gamma}{\Gamma} \geq 2Br(B_s^0 \rightarrow D_s^{(*)-} D_s^{(*)+}) \geq 0.012$$

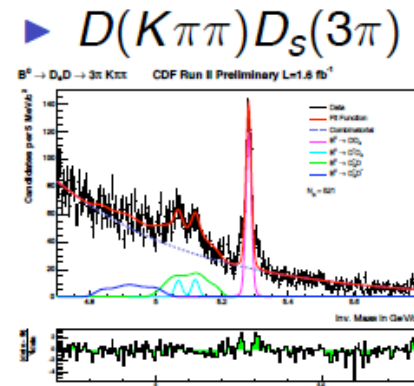
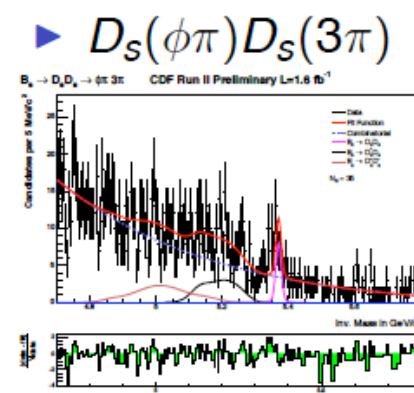
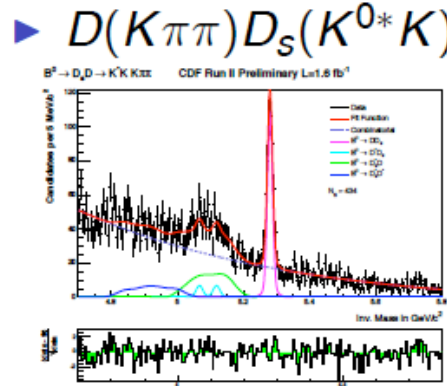
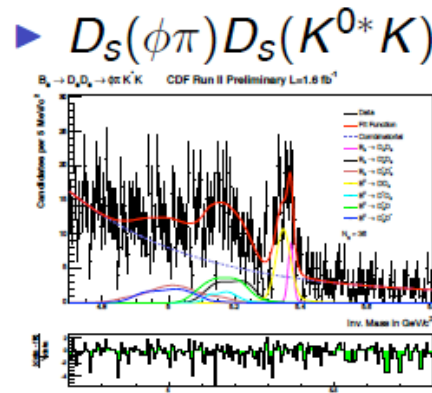
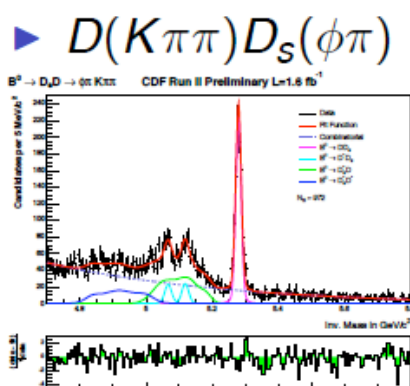
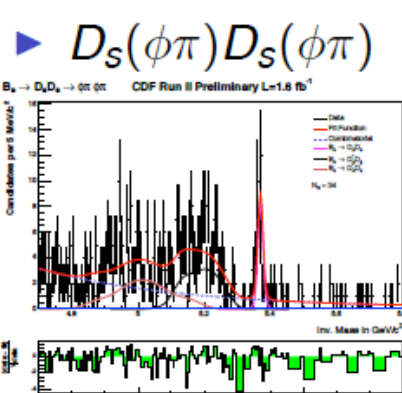
Phys.Rev.Lett. 100:021803,2008.

• New Analysis on going.

• New Neural Network Selection to increase acceptance (in 1.6 fb^{-1}):

$\sim 105 B_s \rightarrow D_s D_s$

$\sim 1930 B_d \rightarrow D D_s$



CP Specific: $B_s \rightarrow KK$

- First Measurement of $B_s \rightarrow KK$ lifetime performed in 360 pb^{-1} . $B_s \rightarrow KK$ extracted using a Maximum Likelihood fit that combines kinematics and particle identification information
- Lifetime measurement interesting since $\sim 95\%$ CP even
- $B \rightarrow hh$ decays can be resolved at CDF
 - Displaced track trigger
 - Good mass resolution

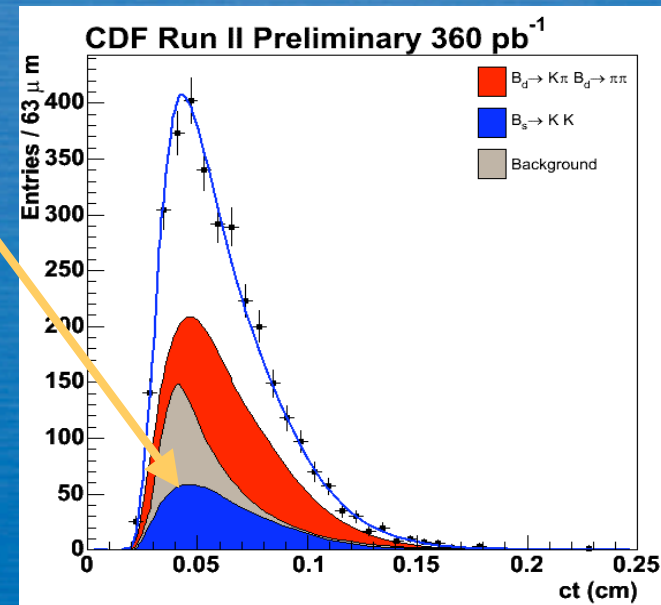
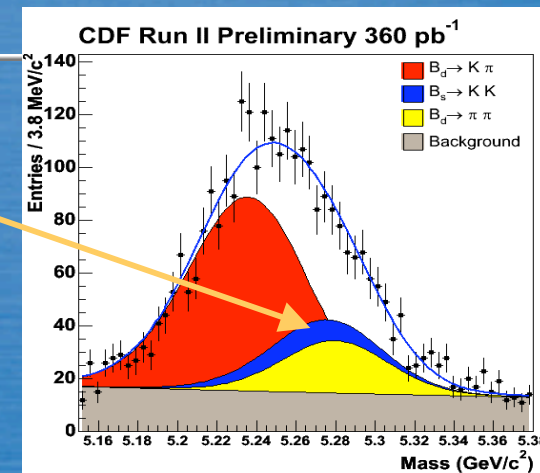
$$\tau(B_s \rightarrow K^+K^-) = 1.53 \pm 0.18(\text{stat}) \pm 0.02(\text{sys}) \text{ ps}$$

Use HFAG flavour specific $\tau = 1.454 \pm 0.040 \text{ ps}$

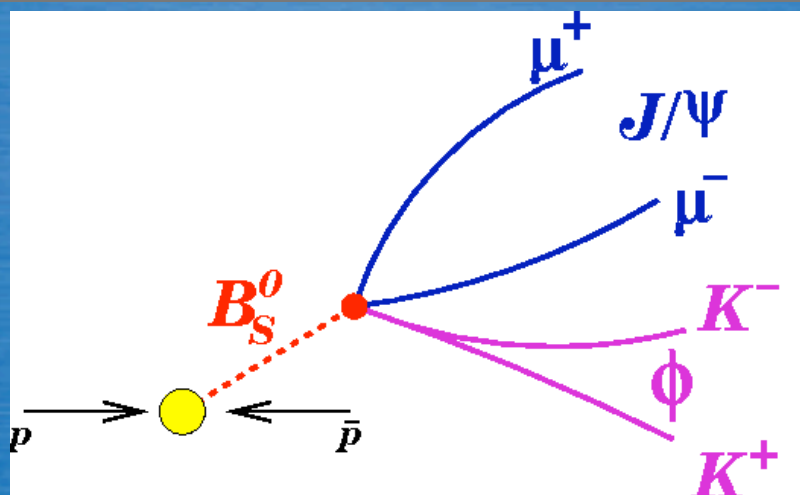
$$360 \text{ pb}^{-1} \frac{\Delta\Gamma}{\Gamma} = -0.08 \pm 0.23(\text{stat}) \pm 0.03(\text{sys})$$

http://www-cdf.fnal.gov/physics/new/bottom/060126.blessed-BsKK_lifetime/

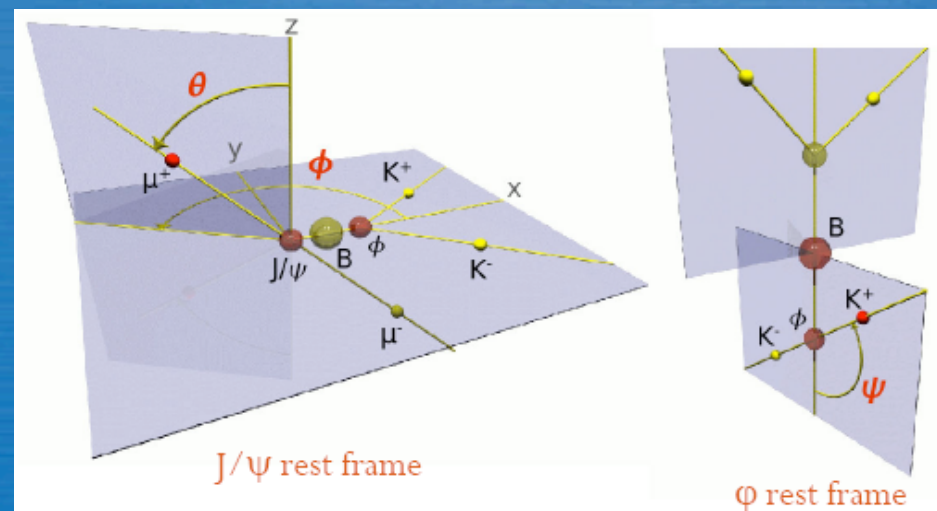
In 2fb^{-1} we expect:
 τ stat error 0.06-0.09ps



$B_s \rightarrow J/\psi \phi$



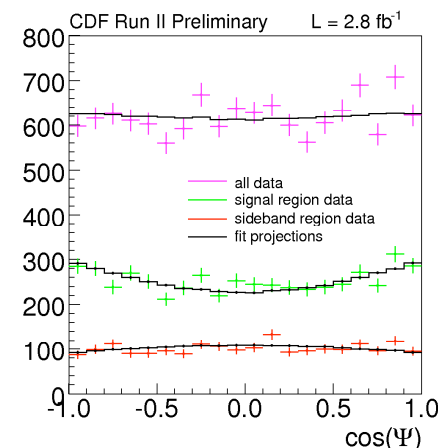
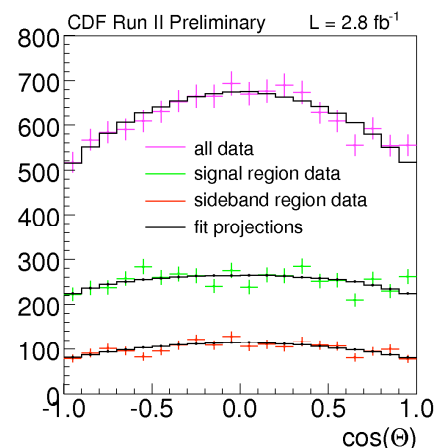
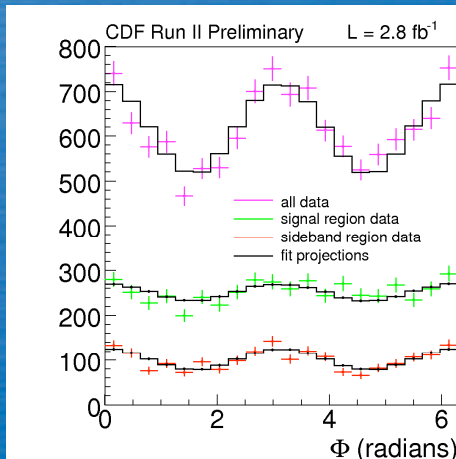
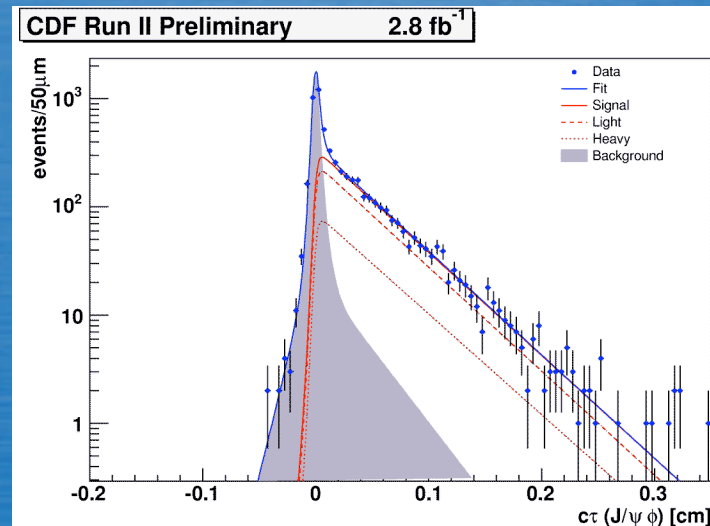
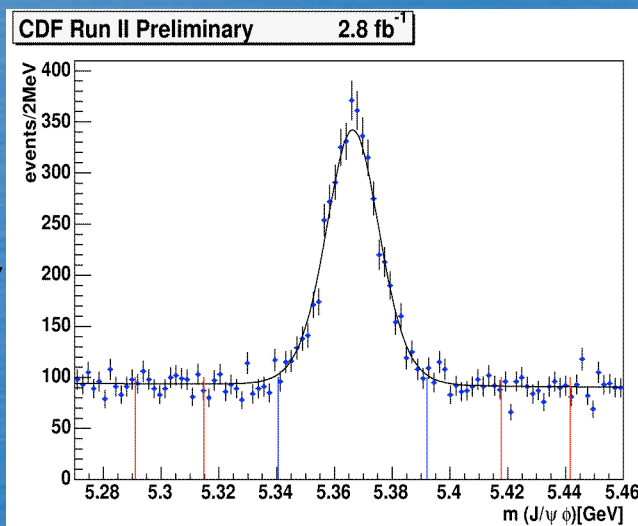
- three decay angles $\vec{p} = (\theta, \phi, \psi)$ describe directions of final decay products



- Extremely physics rich decay mode
- Can measure lifetime, **decay width difference $\Delta\Gamma$** and **CP violating phase β_s**
- Decay of B_s (spin 0) to J/ψ (spin 1) ϕ (spin 1) leads to three different angular momentum final states:
 - $L = 0$ (s-wave), 2 (d-wave) \rightarrow CP even (\approx short lived or light B_s if $\Phi_s \approx 0$)
 - $L = 1$ (p-wave) \rightarrow CP odd (\approx long lived or heavy B_s if $\Phi_s \approx 0$)

Tagged $B_s \rightarrow J/\psi\phi$: $\Delta\Gamma$

- Performed simultaneous **mass, lifetime and angular fit**
- CDF reconstructed around **3200 events** in 2.8 fb^{-1} using selections based on **Neural Network**.



Tagged $B_s \rightarrow J/\psi\phi$: $\Delta\Gamma$

Assume No CP violation
In 2.8 fb^{-1} :

$$c\tau_s = 459 \pm 12 \text{ (stat)} \pm 3 \text{ (sys)} \mu\text{m}$$

$$\Delta\Gamma = 0.02 \pm 0.05 \text{ (stat)} \pm 0.01 \text{ (sys)} \text{ ps}^{-1}$$

$$|A_0|^2 = 0.508 \pm 0.024 \text{ (stat)} \pm 0.008 \text{ (sys)}$$

$$|A_{//}|^2 = 0.241 \pm 0.019 \text{ (stat)} \pm 0.007 \text{ (sys)}$$

Predicted $\Delta\Gamma$
 $0.096 \pm 0.039 \text{ ps}^{-1}$
(arxiv: 0802.0977)

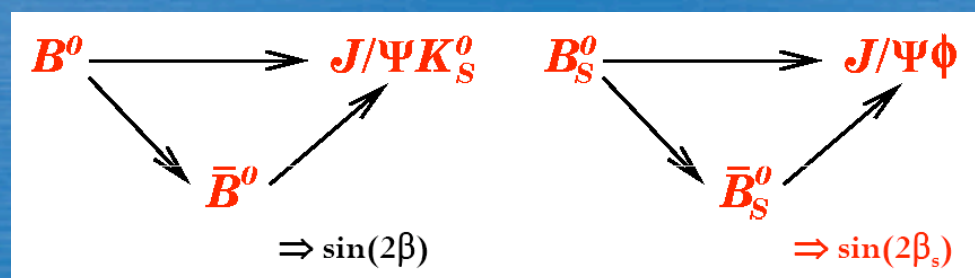
This result with 2.8 fb^{-1} :

http://www-cdf.fnal.gov/physics/new/bottom/080724.blessed-tagged_BsJPsiPhi_update_prelim/

Published analysis with 1.7 fb^{-1} : Phys. Rev. Lett. 100, 121803 (2008)

Add Flavor Tagging

CP Violation Phase β_s in $B_s \rightarrow J/\psi\phi$



$$\beta_s^{\text{SM}} = \arg(-V_{ts}V_{tb}^*/V_{cs}V_{cb}^*) \approx 0.02$$

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

- CP violation phase β_s in SM is predicted to be very small, $O(\lambda^2)$
 → New Physics CPV can compete or even dominate over small Standard Model CPV
- Ideal place to search for New Physics

CP Violation Phase β_s in Tagged $B_s \rightarrow J/\psi\phi$



- Likelihood expression predicts better sensitivity to β_s but still double minima due to symmetry:

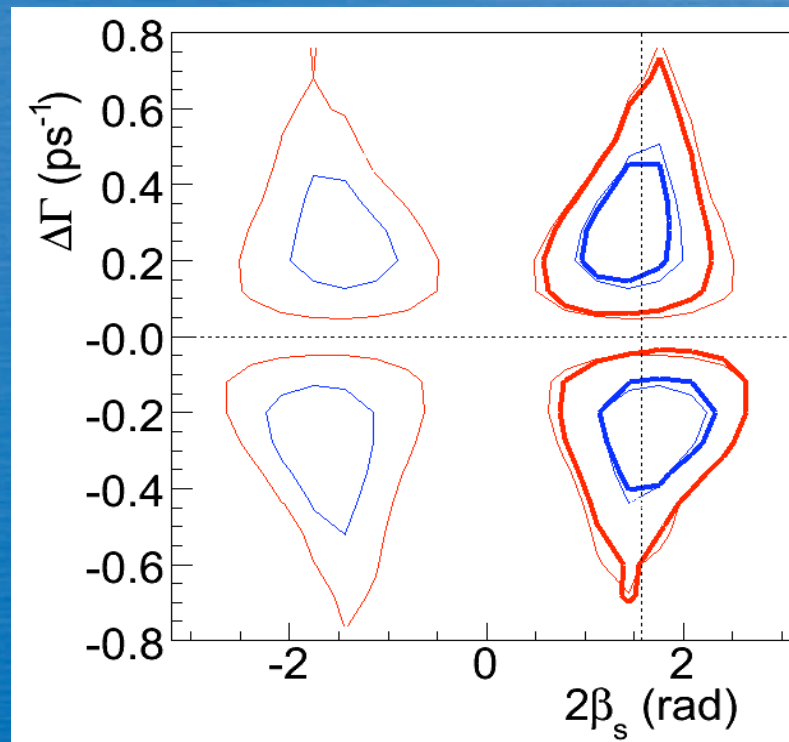
$$2\beta_s \rightarrow \pi - 2\beta_s$$

$$\Delta\Gamma \rightarrow -\Delta\Gamma$$

$$\delta_{\parallel} \rightarrow 2\pi - \delta_{\parallel}$$

$$\delta_{\perp} \rightarrow \pi - \delta_{\perp}$$

pseudo experiment $2\beta_s$ - $\Delta\Gamma$ likelihood profile



strong phases
can separate
the two minima

- Study expected effect of tagging using pseudo-experiments

- Improvement of parameter resolution is small due to limited tagging power ($\epsilon D^2 \sim 4.5\%$ compared to B factories $\sim 30\%$)

- However, $\beta_s \rightarrow -\beta_s$ no longer a symmetry

→ 4-fold ambiguity reduced to 2-fold ambiguity

→ allowed region for β_s is reduced to half

$$2\Delta\log(L) = 2.3 \approx 68\% \text{ CL}$$

$$2\Delta\log(L) = 6.0 \approx 95\% \text{ CL}$$

— un-tagged

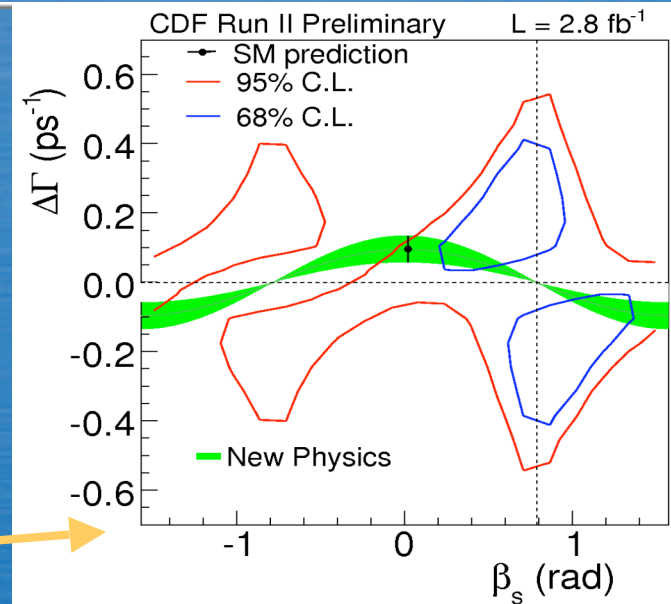
— tagged

CP Violation Phase β_s in Tagged $B_s \rightarrow J/\psi\phi$



- CDF: Standard Model probability **7%, $\sim 1.8\sigma$**

- HFAG combines **old CDF** (1.4 fb^{-1} , 1.5σ from SM, PRL 100, 161802 (2008))
- DØ (2.8 fb^{-1} , 1.7σ from SM) results yield a 2.2σ deviation from SM (similar results from UFit and CKM)



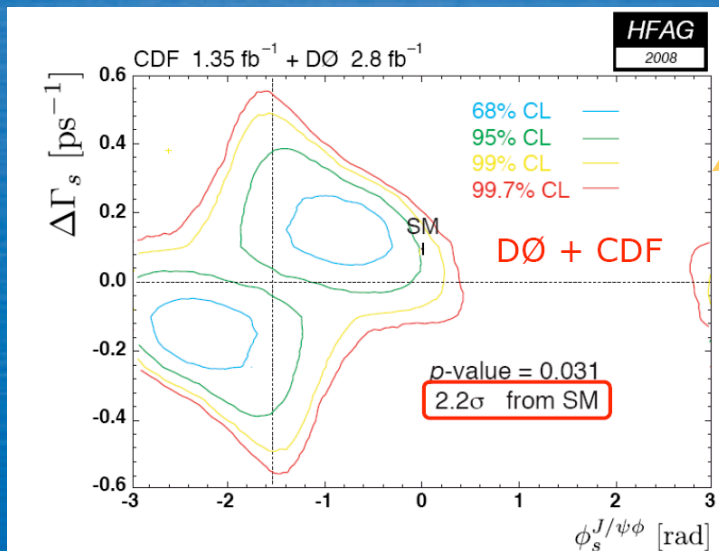
Different Conventions:

ϕ_s

β_s

- Ongoing CDF and DØ work to **produce Tevatron $\Delta\Gamma - \beta_s$ average using 2.8 fb^{-1}**

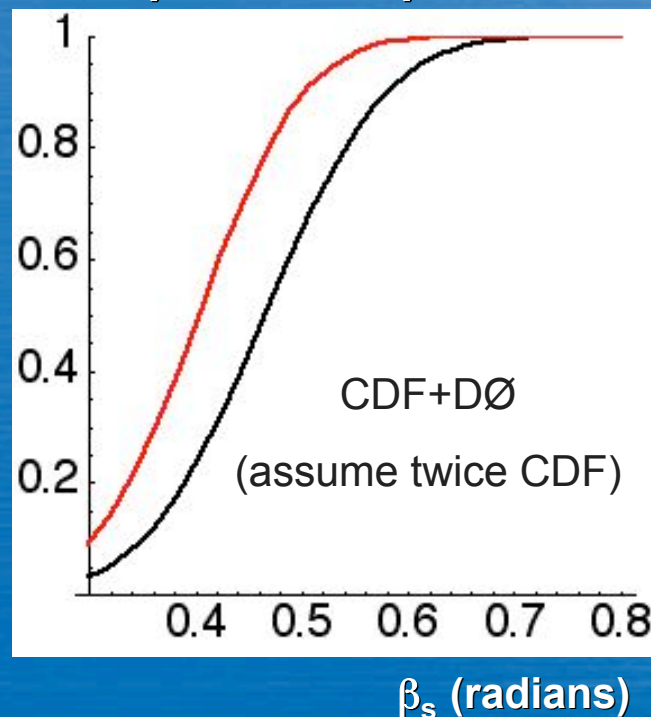
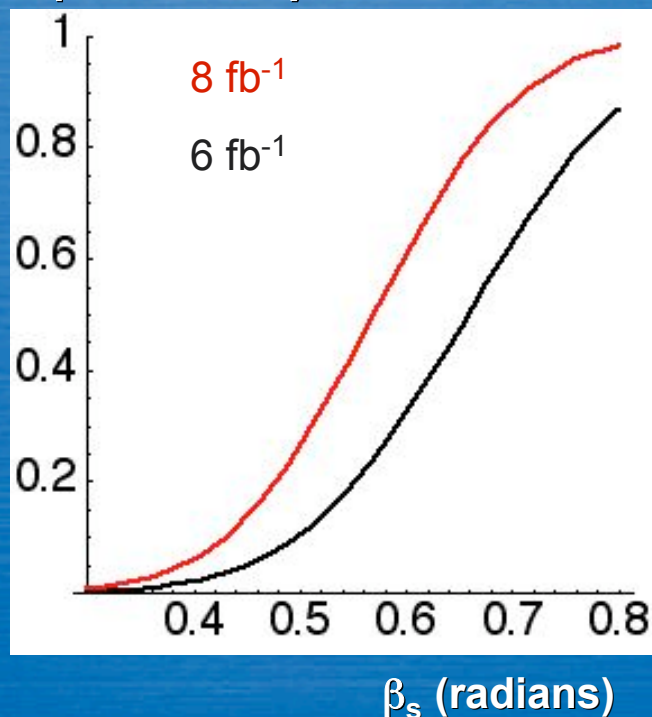
- Investigating two combination methods:
 - combine 2D profile likelihoods
 - will be ready very soon
 - perform simultaneous fit of CDF and DØ data
 - expect to be more powerful, longer timescale



Future

- Tevatron can search for anomalously large values of β_s .
- Shown results with 2.8 fb^{-1} , but more than 5 fb^{-1} already on tape to be analyzed soon with **NEW flavor tagger**.
- Currently considering other improvements.
- Expect 8 fb^{-1} by the end of Run 2 in 2010 (maybe 10 fb^{-1} by end of 2011 ?).

Probability of 5σ observation



If β_s is indeed large combined Tevatron results have good chance to prove it.

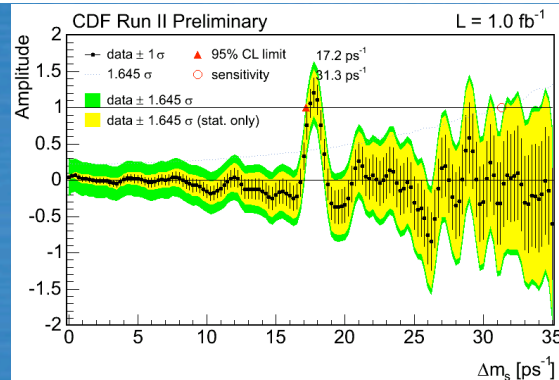


B_s Mixing

CDF Observed B_s Mixing and Measured :

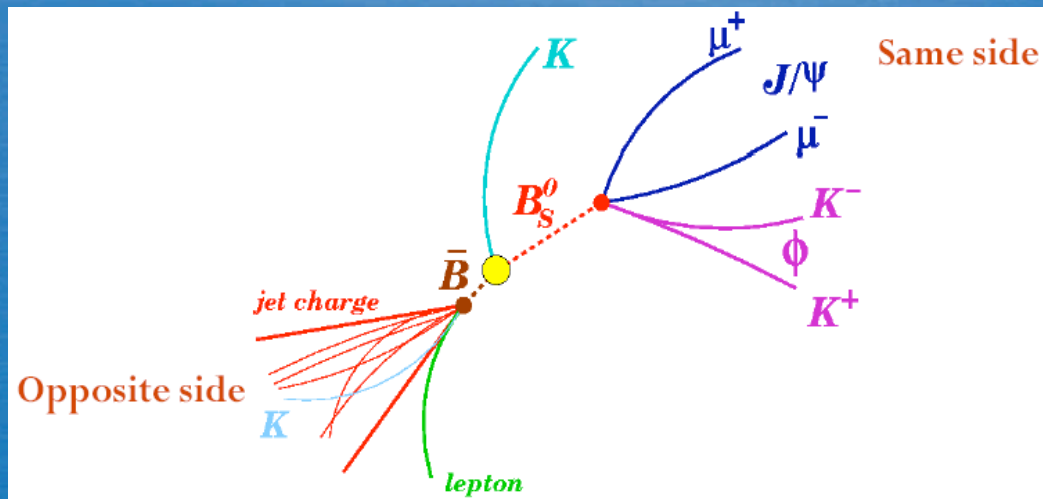
$$\Delta m_s = 17.77 \pm 0.12 \text{ ps}^{-1}$$

PRL 97, 242003 2006



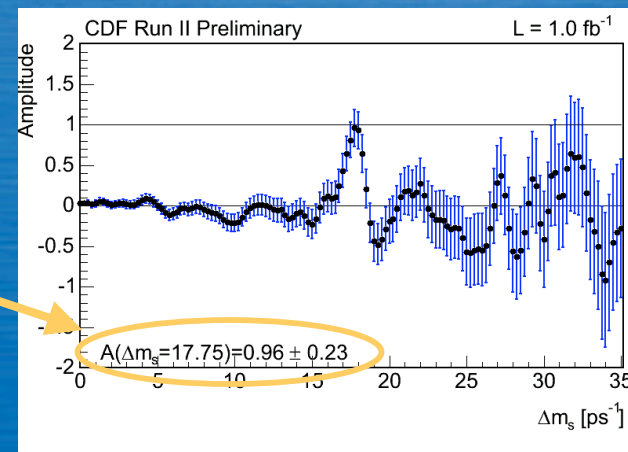
B_s Mixing is now a very important benchmark for flavor tagging calibration

- Tevatron: *b*-quarks mainly produced in *b anti-b*-pairs → flavor of the B meson at production inferred with
- OST: exploits decay products of other *b*-hadron in the event
- SST: exploits the correlations with particles produced in fragmentation



Old Tagger

- OST calibrated on *data* (*B*⁺, *B*⁰)
- SSKT calibrated on *MC*, but checked on B_s mixing measurement
- Combined tagging power at CDF ~4.5% (compared to ~30% at B factories)

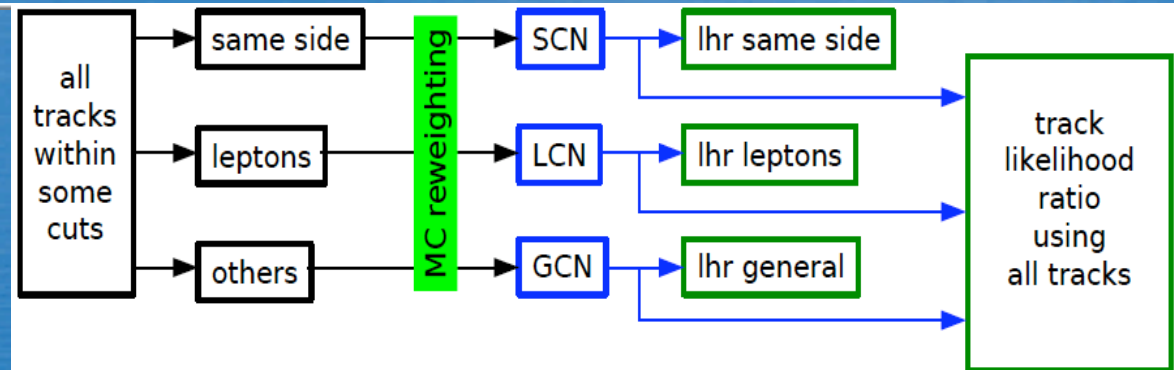


New Tagger Principle

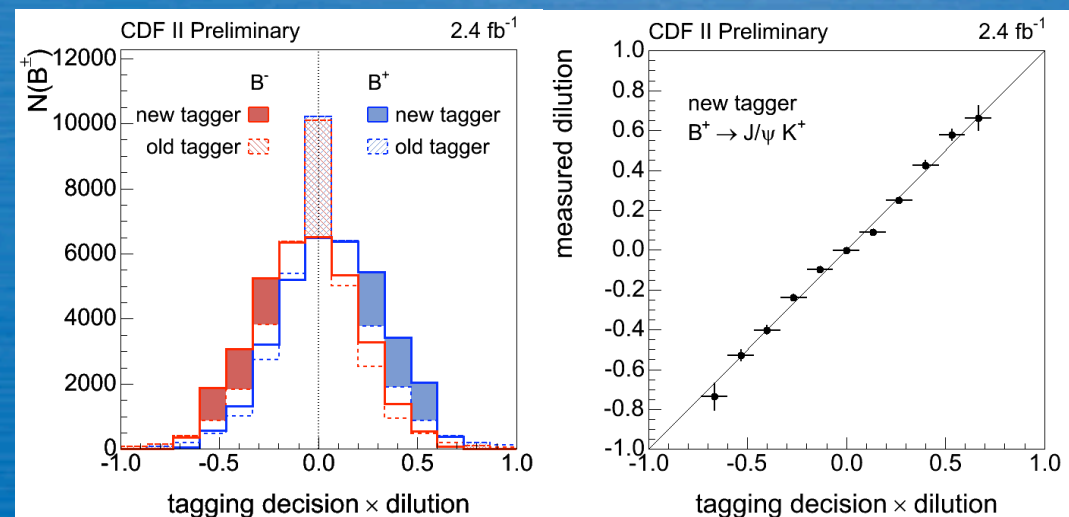


Combine the information from all tracks in the event

- **Same Side:** tracks in the same side in which the same side B was found.
- **Leptons:** tracks that are electron or muon candidate.
- **Others:** all remaining tracks (very low B flavor information).



- **Split** all charged tracks into the three subsamples: **same side**, **leptons** and **others**.
- **Train** an independent “**Track Flavor Correlation Neural Network**” for each subsample
- **Combine** tracks of each subsample in a **separate Likelihood Ratio**



The new Tagger will be calibrated/checked on MC and on **NEW B_s mixing measurement** with higher statistics data samples and used in **NEW tagged $B_s \rightarrow J/\psi \phi$**

Conclusions

- Several ways of measuring $\Delta\Gamma$ have been deployed; to be updated soon:

$$\Delta\Gamma(B_s \rightarrow J/\psi\phi) = 0.02 \pm 0.05(stat) \pm 0.01(sys) ps^{-1}$$

$$\frac{\Delta\Gamma}{\Gamma}(B_s \rightarrow K^+K^-) = -0.08 \pm 0.23(stat) \pm 0.03(sys)$$

$$\frac{\Delta\Gamma}{\Gamma} \geq 2Br(B_s^0 \rightarrow D_s^{(*)-} D_s^{(*)+}) \geq 0.012 \quad (95\% \text{ C.L.})$$

- Significant regions in β_s space are ruled out
- CDF observes 1,8 sigma β_s deviations from SM predictions
- Combined HFAG result 2.2 sigma w.r.t SM expectation
- Soon: updated analyses from CDF with new tagger and more data



Backup Slides

$B_s \rightarrow J/\Psi \Phi$ Decay Rate

- $B_s \rightarrow J/\Psi \Phi$ decay rate as function of **time**, **decay angles** and initial B_s flavor:

$$\begin{aligned} \frac{d^4 P(t, \vec{\rho})}{dt d\vec{\rho}} \propto & |A_0|^2 T_+ f_1(\vec{\rho}) + |A_{||}|^2 T_+ f_2(\vec{\rho}) \\ & + |A_{\perp}|^2 T_- f_3(\vec{\rho}) + |A_{||}| |A_{\perp}| \mathcal{U}_+ f_4(\vec{\rho}) \\ & + |A_0| |A_{||}| \cos(\delta_{||}) T_+ f_5(\vec{\rho}) \\ & + |A_0| |A_{\perp}| \mathcal{V}_+ f_6(\vec{\rho}), \end{aligned}$$

time dependence terms

angular dependence terms

terms with β_s dependence

$$T_{\pm} = e^{-\Gamma t} \times [\cosh(\Delta\Gamma t/2) \mp \cos(2\beta_s) \sinh(\Delta\Gamma t/2) \mp \eta \sin(2\beta_s) \sin(\Delta m_s t)],$$

terms with Δm_s dependence present if initial state of B meson (B vs anti-B) is determined (flavor tagged)

$$\begin{aligned} \mathcal{U}_{\pm} = \pm e^{-\Gamma t} \times & [\sin(\delta_{\perp} - \delta_{||}) \cos(\Delta m_s t) \\ & - \cos(\delta_{\perp} - \delta_{||}) \cos(2\beta_s) \sin(\Delta m_s t) \\ & \pm \cos(\delta_{\perp} - \delta_{||}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2)] \end{aligned}$$

$$\begin{aligned} \mathcal{V}_{\pm} = \pm e^{-\Gamma t} \times & [\sin(\delta_{\perp}) \cos(\Delta m_s t) \\ & - \cos(\delta_{\perp}) \cos(2\beta_s) \sin(\Delta m_s t) \\ & \pm \cos(\delta_{\perp}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2)]. \end{aligned}$$

'strong' phases:

$$\delta_{||} \equiv \text{Arg}(A_{||}(0) A_0^*(0))$$

$$\delta_{\perp} \equiv \text{Arg}(A_{\perp}(0) A_0^*(0))$$

Analysis without Flavor Tagging

- Drop information on production flavor
- Simpler but less powerful analysis

$$\mathcal{T}_{\pm} = e^{-\Gamma t} \times [\cosh(\Delta\Gamma t/2) \mp \cos(2\beta_s) \sinh(\Delta\Gamma t/2) \mp \cancel{\eta \sin(2\beta_s) \sin(\Delta m_s t)}],$$

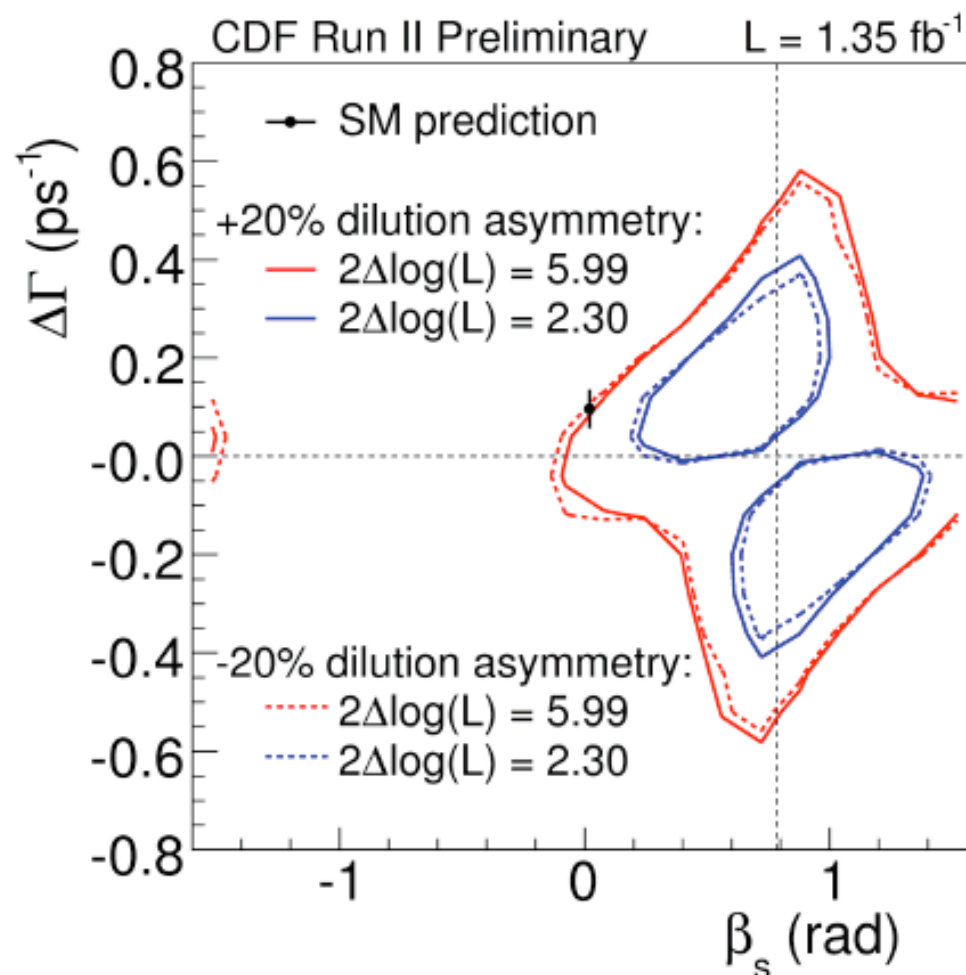
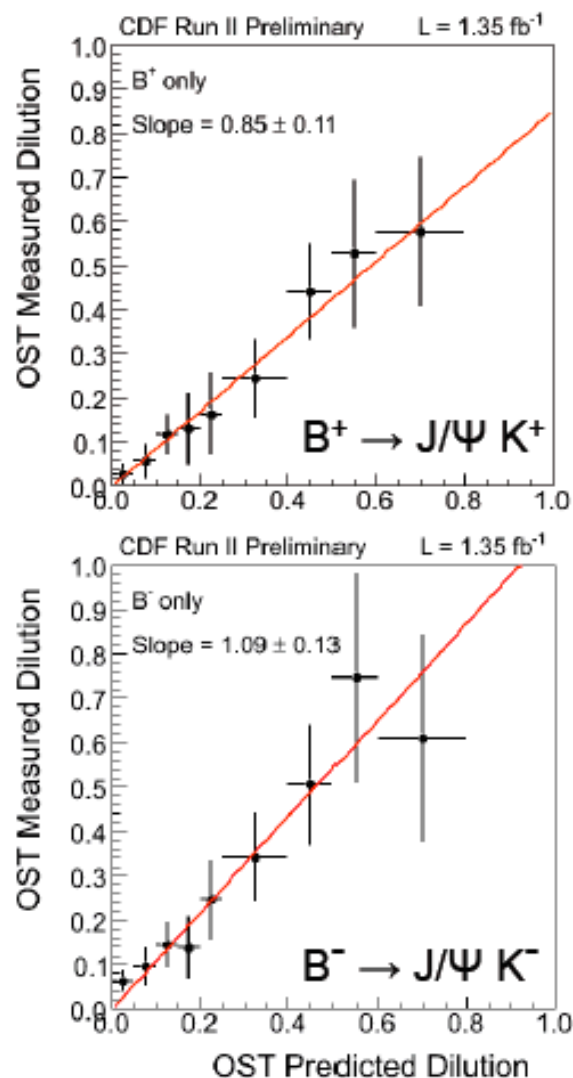
$$\mathcal{U}_{\pm} = \pm e^{-\Gamma t} \times [\sin(\delta_{\perp} - \delta_{\parallel}) \cos(\Delta m_s t) - \cancel{\cos(\delta_{\perp} - \delta_{\parallel}) \cos(2\beta_s) \sin(\Delta m_s t)} \pm \cos(\delta_{\perp} - \delta_{\parallel}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2)]$$

$$\mathcal{V}_{\pm} = \pm e^{-\Gamma t} \times [\cancel{\sin(\delta_{\perp}) \cos(\Delta m_s t)} - \cancel{\cos(\delta_{\perp}) \cos(2\beta_s) \sin(\Delta m_s t)} \pm \cos(\delta_{\perp}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2)].$$

- Still sensitive to CP-violation phase β_s
- Suited for precise measurement of width-difference and average lifetime

Effect of Dilution Asymmetry on β_s

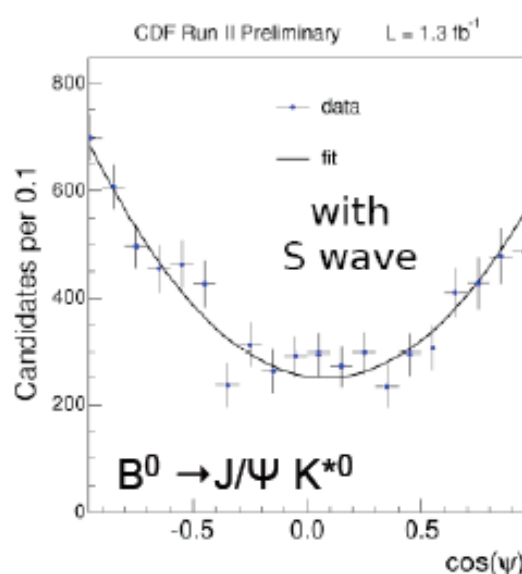
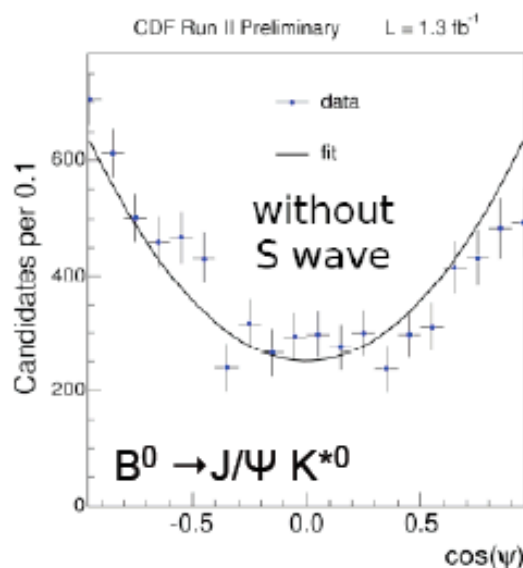
- Effect of 20% b-bbar dilution asymmetry is very small



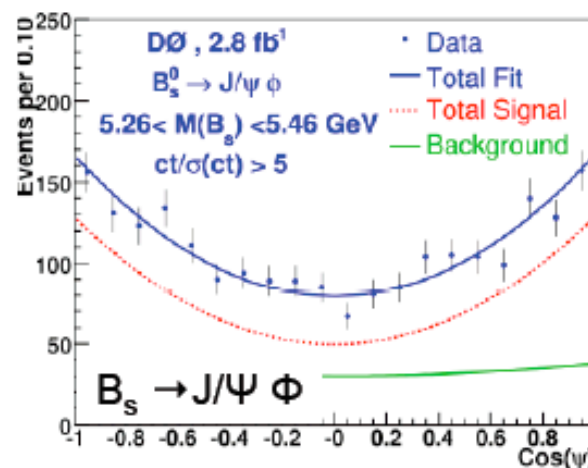
S-wave Effect on Measurement of CP Violating Phases ?

S.Stone, L.Zhang, arXiv:0812.2832

- What is effect of interference between S-wave $B_s \rightarrow J/\psi f^0$ or $B_s \rightarrow J/\psi K^+K^-$ (non-resonant) and $B_s \rightarrow J/\psi \phi$?
- Within statistics, no evidence for f^0 or non-resonant KK S-wave in $\Phi(KK)$ mass distribution
- $\cos(\Psi)$ distribution sensitive to S-wave interference:



Evidence for S-wave in $B^0 \rightarrow J/\psi K^{*0}$

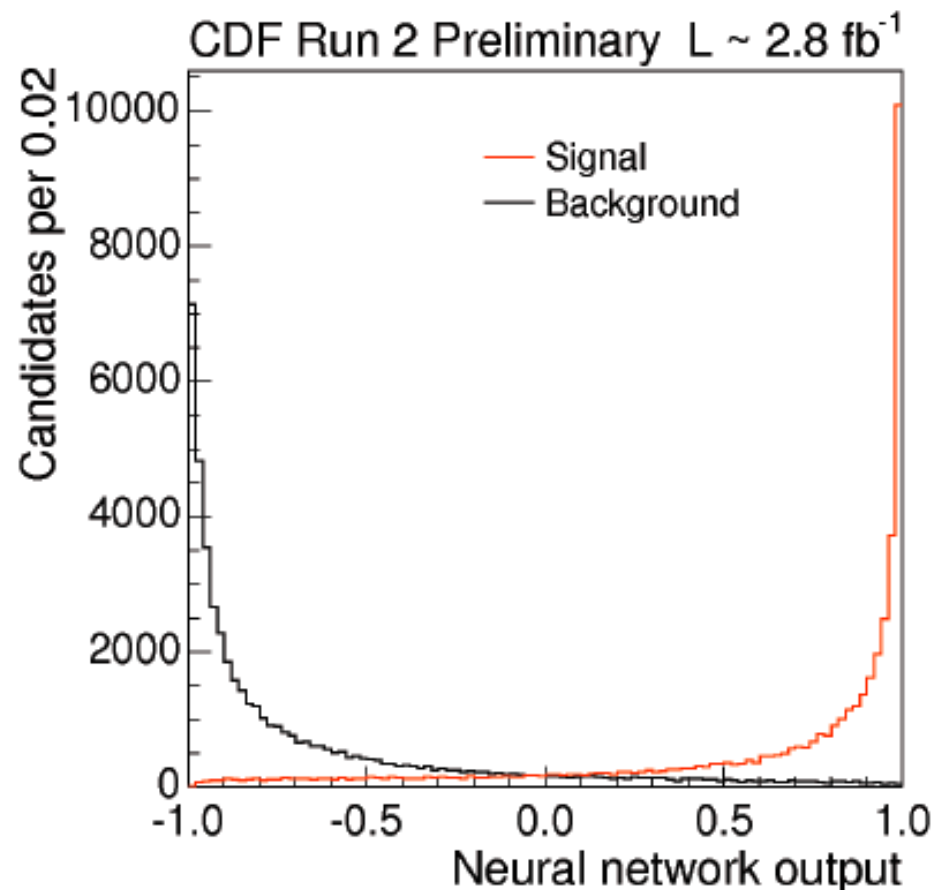


No evidence for S-wave
in $B_s \rightarrow J/\psi \phi$

CDF Selection of B_s Signal Using ANN

- NN maximizes $S/\sqrt{S+B}$, trained on MC for signal and mass sidebands for background

- Variables used by NN
- B_s^0 : use p_T and vertex quality
- J/ψ : use p_T and vertex prob.
- Φ : use mass and vertex quality
- PID (dE/dx + TOF) for Kaons from Φ
- ...



CDF Cross-check on $B^0 \rightarrow J/\psi K^{*0}$

$B^0 \rightarrow J/\psi K^{*0}$: high-statistics test of angular efficiencies and fitter

$$c\tau = 456 \pm 6 \text{ (stat)} \pm 6 \text{ (syst)} \mu\text{m}$$

$$|A_0(0)|^2 = 0.569 \pm 0.009 \text{ (stat)} \pm 0.009 \text{ (syst)}$$

$$|A_{\parallel}(0)|^2 = 0.211 \pm 0.012 \text{ (stat)} \pm 0.006 \text{ (syst)}$$

$$\delta_{\parallel} = -2.96 \pm 0.08 \text{ (stat)} \pm 0.03 \text{ (syst)}$$

$$\delta_{\perp} = 2.97 \pm 0.06 \text{ (stat)} \pm 0.01 \text{ (syst)}$$

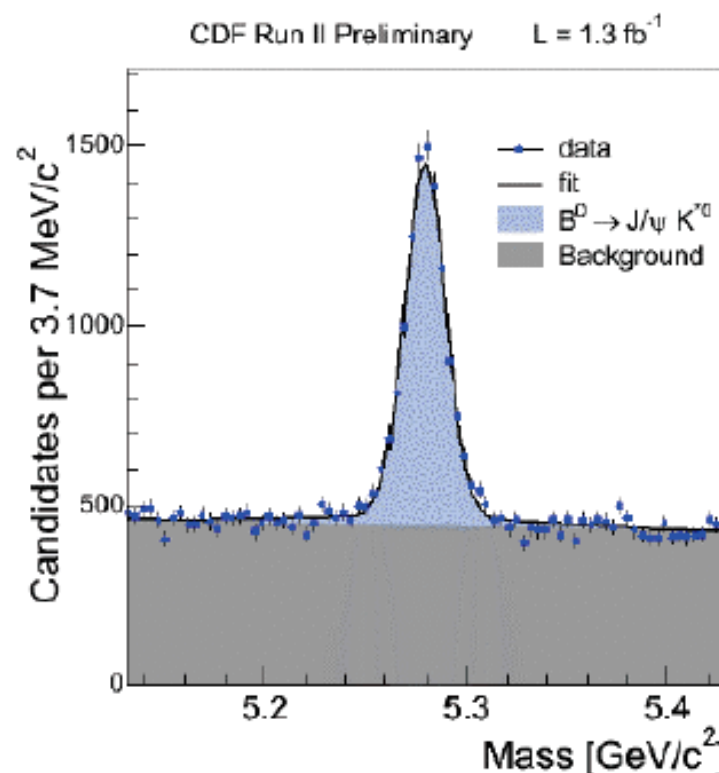
- Not only agree with latest BaBar results, (PRD 76,031102 (2007)) but also competitive

$$|A_0(0)|^2 = 0.556 \pm 0.009 \text{ (stat)} \pm 0.010 \text{ (syst)}$$

$$|A_{\parallel}(0)|^2 = 0.211 \pm 0.010 \text{ (stat)} \pm 0.006 \text{ (syst)}$$

$$\delta_{\parallel} = -2.93 \pm 0.08 \text{ (stat)} \pm 0.04 \text{ (syst)}$$

$$\delta_{\perp} = 2.91 \pm 0.05 \text{ (stat)} \pm 0.03 \text{ (syst)}$$



β_s vs ϕ_s

- Up to now, introduced two **different** phases:

$$\phi_s^{\text{SM}} = \arg\left(-\frac{M_{12}}{\Gamma_{12}}\right) \approx 4 \times 10^{-3} \quad \text{and} \quad \beta_s^{\text{SM}} = \arg(-V_{ts}V_{tb}^*/V_{cs}V_{cb}^*) \approx 0.02$$

- New Physics can affect both phases by **same** quantity ϕ_s^{NP} (A. Lenz, arxiv:0705.3802v2):

$$2\beta_s = 2\beta_s^{\text{SM}} - \phi_s^{\text{NP}}$$

$$\phi_s = \phi_s^{\text{SM}} + \phi_s^{\text{NP}}$$

- If the new physics phase ϕ_s^{NP} dominates over the SM phases: $2\beta_s^{\text{SM}}$ and ϕ_s^{SM}
 → neglect SM phases and obtain:

$$2\beta_s = -\phi_s^{\text{NP}} = -\phi_s$$

β_s Phase and the CKM Matrix

- CKM matrix connects mass and weak quark eigenstates
- Expand CKM matrix in $\lambda = \sin(\theta_{\text{Cabibbo}}) \approx 0.23$

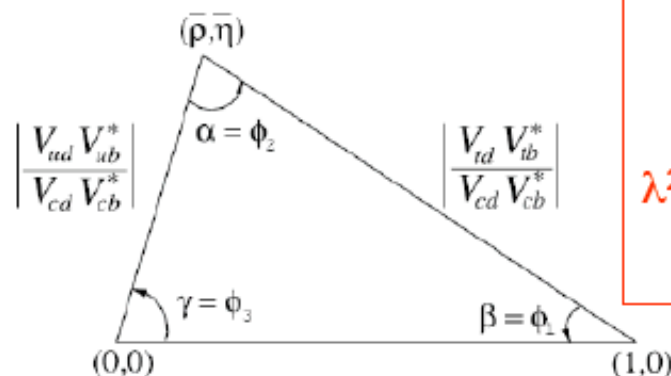
$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \approx \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda + \frac{1}{2}A^2\lambda^5[1 - 2(\rho + i\eta)] & 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4(1 + 4A^2) & A\lambda^2 \\ A\lambda^3[1 - (1 - \frac{1}{2}\lambda^2)(\rho + i\eta)] & -A\lambda^2 + \frac{1}{2}A\lambda^4[1 - 2(\rho + i\eta)] & 1 - \frac{1}{2}A^2\lambda^4 \end{pmatrix}$$

- To conserve probability CKM matrix must be unitary
→ Unitary relations can be represented as “unitarity triangles”

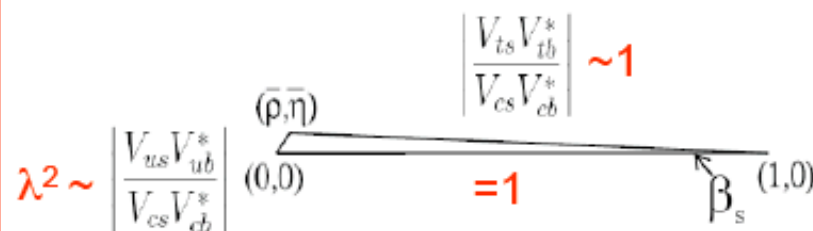
unitarity relations:

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

unitarity triangles:



$$V_{us}V_{ub}^* + V_{cs}V_{cb}^* + V_{ts}V_{tb}^* = 0$$



very small CPV phase β_s of order λ^2 accessible in B_s decays